

Question bank on Classical mechanics and special theory
of relativity
Semester-III

1. (i) Calculate the distance travelled by a particle during one mean life if it travels with a speed of 2.22×10^{10} cm/sec. [Proper mean life = 2.5×10^{-8} s].
(ii) State Einstein's postulate for special theory of relativity which related with Michelson-Morley experiment.
(iii) Using Lorentz transformations obtain the expression for time dilation. What is proper time?
(iv) Obtain the relation between mass and velocity of a relativistic particle.
(v) Hence prove that kinetic energy of the relativistic particle is $T = mc^2 + m_0c^2$ where m_0 is rest mass.
(vi) Obtain Einstein's velocity addition theorem.
Show that Lorentz transformation can be regarded as rotation of axes through an imaginary angle $\theta = \tan^{-1}(i\beta)$ where $\beta = v/c$.

2. (i) What do you mean by holonomic and nonholonomic constraints?
(ii) A particle is constrained to move on a spherical surface. Write down the equation of constraint. Mention the number of degrees of freedom and generalized co-ordinates of the system.
(iii) Show that conjugate momentum of a cyclic coordinate is a conserved quantity.

3. (i) Define virtual displacement and virtual work. State principle of virtual work. Hence obtain D'Alembert principle.
(ii) Write down the Lagrangian of a compound pendulum and hence obtain the Lagrange's equation of motion.

4. (i) Define Hamiltonian of a system. Hence obtain Hamilton's equation of motion.
(ii) Show that the Hamiltonian of a conservative system is total energy of the system.
(iii) Show that the Lagrange's equation of motion remains unaltered if it is added to a constant.

5. (i) Mention whether the constraint $x dy + y dx = c dx + f dy$ is holonomic or not.
(ii) A uniformly heavy flexible string is fixed at two ends. Find the equation of the curve describing the form of the state.

6. (i) The Lagrangian of a system is $L = \dot{q}_1^2 + \dot{q}_2^2 + \dot{q}_1\dot{q}_2 - q_1^2 - q_2^2$. Obtain the equation of motion.
(ii) Prove that total angular momentum of a closed system remain constant in isotropy in space.

- (iii) What is action and Hamilton's principle of least action? Obtain Lagrange's equation of motion from the principle.
7. (i) Obtain Lagrange's equation for a holonomic conservative system from D'Alembert's principle.
- (ii) Show that for a conservative system in which the Lagrangian is not an explicit function of time, Hamiltonian is conserved.